



Investigation of temperature-dependent viscoelastic properties of thermal lesions in *ex vivo* animal liver tissue

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ABSTRACT

The viscoelastic characteristics of thermal lesions in *ex vivo* animal liver are investigated in this paper. Characterization of the moduli of thermal lesions prepared at several temperatures will provide additional information for the elastographic monitoring of radio frequency ablation of hepatic tumors. In this study, the frequency-dependent complex modulus of thermal lesions prepared at temperatures ranging from 60 to 90 °C over a frequency range from 0.1 to 50 Hz are presented. Lesions were prepared using either radio frequency ablation or double immersion boiling. It was found that both the magnitude and phase of the modulus increase with frequency, a behavior that has been noted in the literature. A new result reported shows that the modulus dependence on temperature reveals a local maximum around 70–75 °C corresponding to the temperature at which tissue has released most of its water content. The modulus values at temperatures higher than 70 °C continued to increase, but the extent of increase depend on animal species and other factors.

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1. Introduction

The most widely utilized method to detect lesions in organs such as the breast, liver, and prostate is through manual palpation. Palpation is effective because pathologic differences are generally well correlated with stiffness changes (Fung, 1993). However, this method is less effective in detecting small lesions, or lesions deep within the body. Many lesions are also isoechoic, meaning that they may not be detectable using ultrasound (US). Studies have both shown examples of tumors in the breast and prostate not visible in standard ultrasound examinations, even though they were significantly stiffer than surrounding tissue (Garra et al., 1997; Hall and Zhu, 2003).

Recent improvements in elastography have made it possible to characterize lesion stiffness and improve strain contrast (i.e., the ratio of the average strain of an inclusion in an elastogram to that of the average background) to provide additional information, since echogenicity and lesion stiffness are uncorrelated (Bharat et al., 2005; Ophir et al., 1991; Varghese et al., 2001). In recent papers (Bharat et al., 2005; Kiss et al., 2004), researchers have studied the variation in the strain contrast and Young's modulus of thermally coagulated lesions in healthy canine liver tissue as a function of temperature and duration of heating. The strain

contrast of lesions prepared using radio frequency (RF) ablation was found to depend on ablation temperature as well as duration of ablation. Strain contrast in elastography depends in part on the modulus contrast, defined as the ratio of the Young's modulus of the lesion to that of the background (Kallel et al., 1996; Ophir et al., 2001), and there is some interest in determining whether the viscoelastic characteristics of lesions of soft tissues will be useful in analyzing strain contrast. A large modulus contrast in the underlying tissue will result in a large strain contrast on the estimated axial strain image. This may have potential utility to provide improved strain imaging capability for minimally invasive methods for treatment of liver cancer, such as RF or microwave ablation (Varghese et al., 2002; Bharat et al., 2008). Currently, the procedure is typically monitored using ultrasound imaging (Varghese et al., 2002; Bharat et al., 2008), but it may be possible to improve the procedure by monitoring with MR elastography (Sinkus et al., 2007; Stafford et al., 1998; Wu et al., 2001).

In this study, viscoelastic characteristics of *ex vivo* canine and porcine liver are investigated using dynamic mechanical analysis (DMA) techniques. These methods have been used extensively in order to characterize mechanical characteristics of many different types of tissue and tissue mimicking materials. The proceeding list of papers includes, but is not limited to, several key examples, that are enumerated by tissue type. Bajema et al. (2000) reported on measurements in red apples (fruit). However, much of the measurements in biological tissue was performed on brain tissue (Cheng and Bilston, 2007; Darvish and Crandall, 2001; Hrapko et al., 2006, 2008). Other biological tissues that have been tested

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include, collagenous (Chen and Humphrey, 1998), ocular (Fritz et al., 1999), and fatty tissue (Geerligts et al., 2008). Results have also been reported from tissue in the kidney (Nasseri and Bilston, 2002), liver (Moffitt et al., 2002; Yeh et al., 2002), prostate (Hoyt et al., 2008a,b), throat (Chan, 2001; Yang et al., 2006) and uterine tissue (Kiss et al., 2006).

In addition, several studies have been conducted either to demonstrate data acquisition methods and analysis or in support of other studies, and may have used tissue or tissue mimicking materials. For example general DMA methods are described in the following papers (Chen et al., 1996; Erkamp et al., 1998; Sammani et al., 2003; Sacks and Sun, 2003), while Ottensmeyer et al. (2004) discusses the impact of the DMA environment on the measurements, and Taylor et al. (2002) present DMA results that support other methods.

Both normal tissue and the thermal lesions created were subjected to low amplitude periodic compressions, and the resulting complex moduli determined. The modulus of the tissue is an important factor in determining strain contrast in elastography, and the long-range goals of this project are to improve the understanding of the relationship between strain contrast and tissue characteristics, and to determine if tissue viscoelastic characteristics can be used effectively to exploit a new contrast mechanism in quasi-static and low frequency elastography.

2. Materials and methods

Determination of the complex moduli in excised tissue specimens is a straightforward procedure. Although there are more rigorous treatments in the literature (Christensen, 1982; Fung, 1993; Lakes, 1998), the basic derivation is summarized here. When a viscoelastic material is deformed, it responds with some level of strain. Expressed in terms of a Stieltjes integral, the stress σ is related to the strain ε (deformation) by the following constitutive relation:

$$\sigma(t) = \int_{-\infty}^t E(t - \tau) \frac{d\varepsilon(\tau)}{d\tau} d\tau, \quad (1)$$

where the relaxation function, $E(t)$, represents the mechanical properties of the material. For the sake of simplicity the material is assumed to be linearly viscoelastic and isotropic. If the applied strain or perturbation is periodic,

$$\varepsilon(t) = \varepsilon_0 e^{i\omega t}, \quad (2)$$

where ε_0 is the peak-to-peak strain amplitude and ω is the frequency, and then the stress response will also be periodic, shifted by some phase angle δ

$$\sigma(t) = \sigma_0 e^{i(\omega t + \delta)}, \quad (3)$$

where σ_0 is the peak-to-peak stress amplitude. Substituting Eqs. (2) and (3) into (1), solving, and performing a Fourier transform on the result produces

$$\sigma(\omega) = E^*(\omega)\varepsilon(\omega), \quad (4)$$

where $E^*(\omega)$ is the frequency-dependent complex modulus of the material. Accounting for the phase shift presented in Eq. (3), $E^*(\omega)$ is expressed as

$$E^*(\omega) = \frac{\sigma_0}{\varepsilon_0} (\cos \delta + i \sin \delta), \quad (5)$$

where the frequency-dependence by δ is implied (i.e., $\delta(\omega)$). The real part of Eq. (5) is known as the storage modulus and reflects the ability of the material to store energy during a loading cycle. The imaginary part is called the loss modulus and indicates the amount of energy lost during each cycle. While the real and imaginary parts can be easily determined, it is more common to present the data in terms of the magnitude and phase, given by $|E^*(\omega)|$ and $\tan \delta$, respectively.

The complex modulus contrast, as introduced by Kiss et al. (2006, 2004), is defined as the ratio of the frequency-dependent complex modulus of an inclusion to that of the background, and is defined by

$$C_t^*(\omega) = \frac{E_{inclusion}^*(\omega)}{E_{background}^*(\omega)}, \quad (6)$$

In general, $C_t^*(\omega)$ is a complex quantity, but our previous studies have shown that the imaginary part is approximately zero. This number can be therefore represented by taking the magnitudes of the two moduli, resulting in a real quantity. For the studies presented, the “inclusion” subscript in the numerator of Eq. (6) refers to a lesion, while the “background” refers to normal tissue.

Ten canine and ten porcine livers were obtained from unrelated studies in an adjacent laboratory. Thermally coagulated regions were prepared using one of two

methods. In the first method, RF ablation was utilized to create thermal lesions in bulk tissue. A multi-prong electrode connected to a Rita Model 1500 (Rita Medical Systems, Inc., Mountain View, CA) was used to create these lesions at 70, 80, and 90 °C for an ablation duration of 10 min. After the lesion was created in tissue, a sample was carefully excised using a custom-made cylindrical cutting tool 20 mm in diameter. The sample was then sliced to an appropriate thickness (3–5 mm). Care was taken to ensure that the ratio of sample thickness to sample diameter was 0.25 or less. This was done to prevent buckling of the sample during testing (Krouskop et al., 1998). After the lesion sample was cut from the bulk tissue, it was placed in isotonic saline for at least 1 h and refrigerated prior to testing. While this method of preparation was adequate for the experiments, it is possible that improved results may be obtained by following a protocol similar to that presented by Ottensmeyer et al. (2004).

Samples prepared using RF ablation, were often too small for mechanical testing at the lower ablation temperatures and ablation durations and difficult to prepare, so, a second method was employed to create thermally coagulated regions. In addition, it was difficult to assure uniformly ablated regions with RF ablation. The second method, termed double immersion boiling (DIB), ensured that there would be more material to work with in order to prepare the samples. The term “boiling” is used here in spite of the fact that water temperatures never exceeded 90 °C. In double immersion boiling, tissue specimens, approximately $4 \times 3 \times 2 \text{ cm}^3$ were immersed in a bath of distilled water. The reservoir was contained by a tin can, which was immersed in a distilled water reservoir. A temperature controller set to the target temperature (60–90 °C in 5 °C intervals), was also immersed in the reservoir. The water was allowed to reach the target temperature before the tissue was immersed in the bath. Tissue specimens were cooked for 15 min to ensure thorough coverage. After the specimen had been in the bath for the allotted time, it was removed and placed in a bath of room temperature distilled water for 5 min. Samples were then cut from the sample and placed in isotonic saline in the manner described above. It should be emphasized that the DIB method is not intended as a replacement method for preparing tissue for viscoelastic characterization. Modeling the mechanical characteristics of lesions is best accomplished using the results from RF ablation. This new method is intended as an approximation to RF ablation and is useful for the aforementioned reasons. This method has been used previously in a study by Techavipoo et al. (2004, 2002).

Viscoelastic characteristics were measured using an EnduraTEC ELF 3220 (Bose/EnduraTEC, Minnetonka, MN), as shown in Fig. 1. The ELF 3220 is a tabletop testing system capable of dynamic testing frequencies from 10^{-5} to 400 Hz used to characterize the viscoelastic properties of materials. The system is electromagnetic, and relies on rare-earth magnets placed in the field created by stationary windings to produce a linear force proportional to the field polarity and intensity.

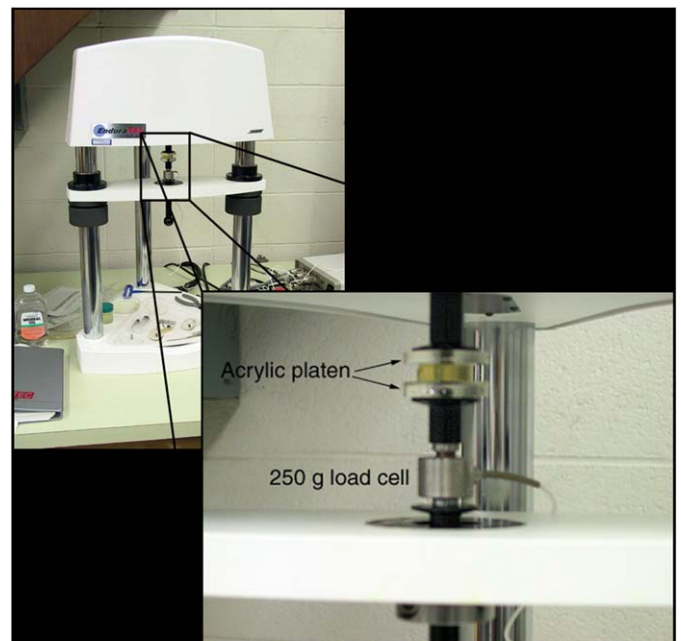


Fig. 1. Photographs of ELF system. The ELF3220 is a tabletop dynamic testing system capable of mechanical testing at frequencies from 10^{-5} to 400 Hz. Load cells of varying sensitivity (50–1000 g) can be used depending on the nature of the samples being studied. The enlargement shows the arrangement of the mover, a sample, and a 250 g load cell. Two acrylic platens ensure full contact on the sample.

Acrylic platens were mounted to both the mover and a calibrated load cell, rated to 250 gm. The platens were then coated with mineral oil to promote free-slip conditions between the sample and the platens. The specimens were subjected to periodic strains from 0.1 to 50 Hz with peak-to-peak amplitude of 1%. Samples were preloaded via compression to 1% to ensure that they would maintain full contact with both platens. All measurements were performed at room temperature (21.0 ± 1.5 °C). For each testing frequency, the sample was held at a mean strain level (1.5%) for 5 sec, after which the mover oscillated at the testing frequency. The system oscillated for 3–20 s (depending on the testing frequency) prior to data acquisition to allow for transient decay, preconditioning, and for the system to achieve the proper amplitude. Values for the complex modulus were obtained using the dynamic mechanical analysis software for the ELF.

Unlike the previous work (Kiss et al., 2004) the testing frequency was limited to 50 Hz. It has been discussed that shear tests provide more accurate results at higher frequencies (Madsen et al., 2008). Furthermore, although the amount of strain applied to the tissues in this study assumes a linearly viscoelastic response, the results may not be useful in estimating behavior at much higher frequencies, such as in the kHz to MHz range. Viscoelastic studies in this realm are best accomplished by techniques that utilize acoustic radiation force imaging (ARFI) and sonoelastography with recent work published by a number of groups (Hoyt et al., 2008a,b; Liu and Ebbini, 2008; Sridhar et al., 2007).

3. Results

Variations of the complex modulus as functions of the mechanical testing frequency, and lesion temperature are presented in this section. Modulus results are presented for RF-ablated canine liver, and for canine and porcine liver prepared with DIB for each of the parameters mentioned above. Fig. 2 shows representative plots of the magnitude (a) and phase (b) of the complex modulus as a function of mechanical testing frequency. The plots here are for canine tissue prepared by RF ablation at 80 °C. Error bars represent the standard error. The range of moduli values in Fig. 2a are from 15 kPa at 0.1 Hz up to 45 kPa at 50 Hz. The values for $\tan \delta$ in the same range, seen in

Fig. 2b run from 0.3 to 0.7. The modulus demonstrates a monotonic increase with frequency, and this behavior was reported in a previous paper, and it is suggestive that the constitutive relation follows a power law (Kiss et al., 2004). This data in this figure is intended to remind the reader of the nature of the modulus' dependence on frequency. This relationship is also noted by other investigators as reported in the literature (Chen et al., 1996; Nasser and Bilston, 2002; Suki et al., 1994; Taylor et al., 2001, 2002, 2003). The phase, while much flatter than the modulus, also increases monotonically with frequency. This too is indicative of power law behavior.

Figs. 3–6 show the dependence of the (a) magnitude and (b) phase of the complex modulus as a function of lesion temperature. It is important to remember that the samples were measured at room temperature, and the lesion temperature value reported indicates the level at which the samples were prepared. In each case, the value for normal tissue has been represented in the graph by adding a data point at 39 °C, since during the animal's life prior to sacrifice it is assumed that the temperature of the liver would have nominally remained near the body temperature.

Fig. 3a shows the modulus dependence on temperature for thermal lesions prepared by RF ablation in canine liver at three frequencies (0.1, 1, and 10 Hz). Although only three lesion temperatures are represented (70, 80, and 90 °C), a local maximum is apparent at 70 °C, with a range of moduli from roughly 18 kPa (at 0.1 Hz) to 35 kPa at 10 Hz. The behavior at the higher temperatures indicates a softening of the tissue (at 80 °C) followed by further stiffening at 90 °C. The phase presented in Fig. 3b behaves in an almost inverse way to the modulus, suggesting that at 80 °C, the tissue has the largest viscoelastic response, with $\tan \delta$ values ranging from 0.3 at 0.1 Hz to 0.55 at 10 Hz. The comparatively lower values of $\tan \delta$ at the other temperatures indicate stiffer responses.

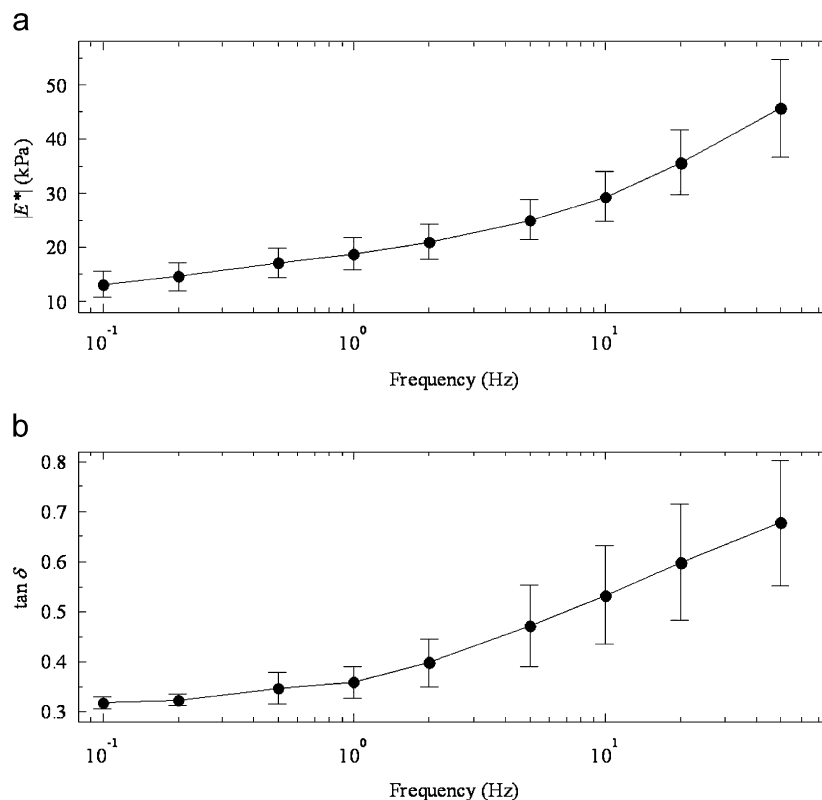


Fig. 2. (a) Magnitude of the complex modulus and (b) $\tan \delta$ as a function of testing frequency for canine tissue prepared by RF ablation at 80 °C. Data points in represent the mean value from specimens taken from ten canine or porcine samples. Error bars in this and subsequent figures represent the standard error.

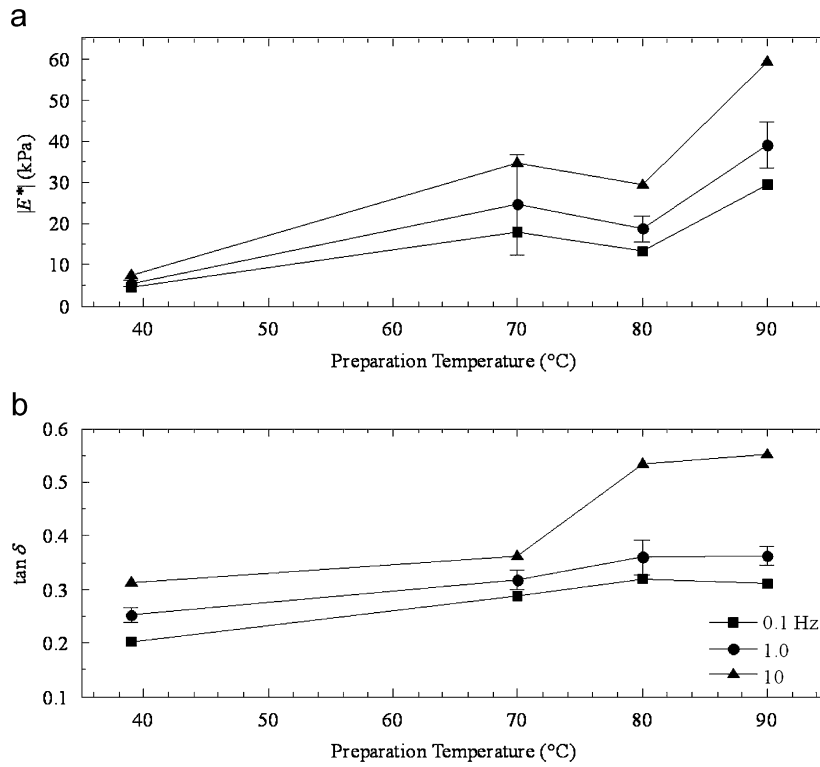


Fig. 3. (a) Magnitude of the complex modulus and (b) $\tan \delta$ as a function of ablation temperature for thermal lesions in canine tissue prepared by RF ablation.

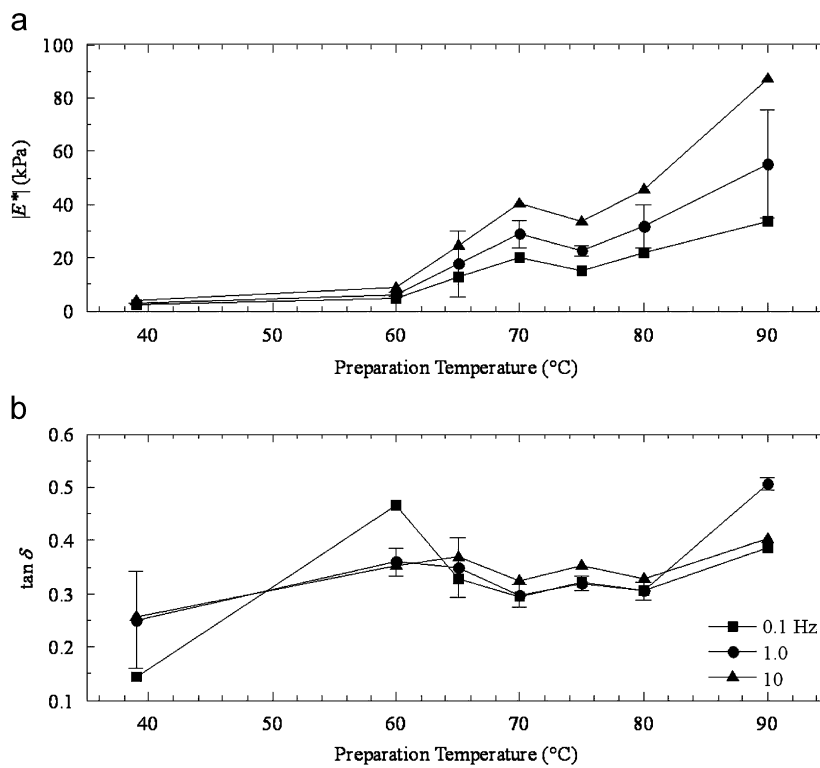


Fig. 4. (a) Magnitude of the complex modulus and (b) $\tan \delta$ as a function of preparation temperature for thermal lesions in canine tissue prepared by double immersion boiling.

The modulus plot in Fig. 4a is similar to those in Fig. 3a, even though the method of tissue preparation is different (DIB). The data is also less sparse, with results presented in 5 °C steps from 60 to 90 °C, with an exception at 85 °C. The local maximum is once

again present at 70 °C and a steady climb from the minimum at 75 °C. Despite the variations, the phase is relatively flat in Fig. 3b, with most points remaining in the narrow range of roughly 0.30–0.40.

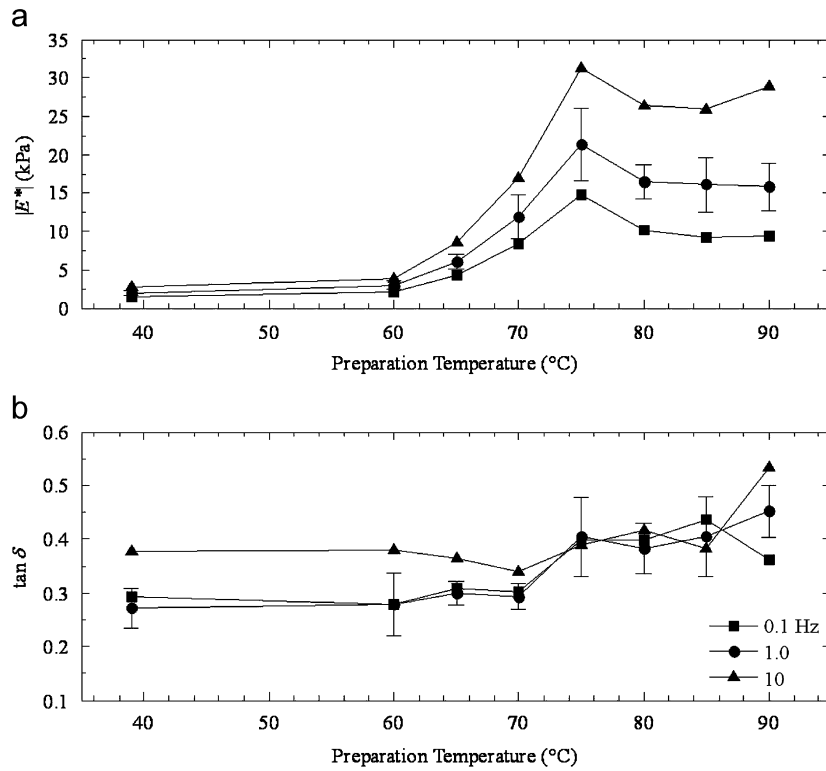


Fig. 5. (a) Magnitude of the complex modulus and (b) $\tan \delta$ as a function of preparation temperature for thermal lesions in porcine tissue prepared by double immersion boiling.

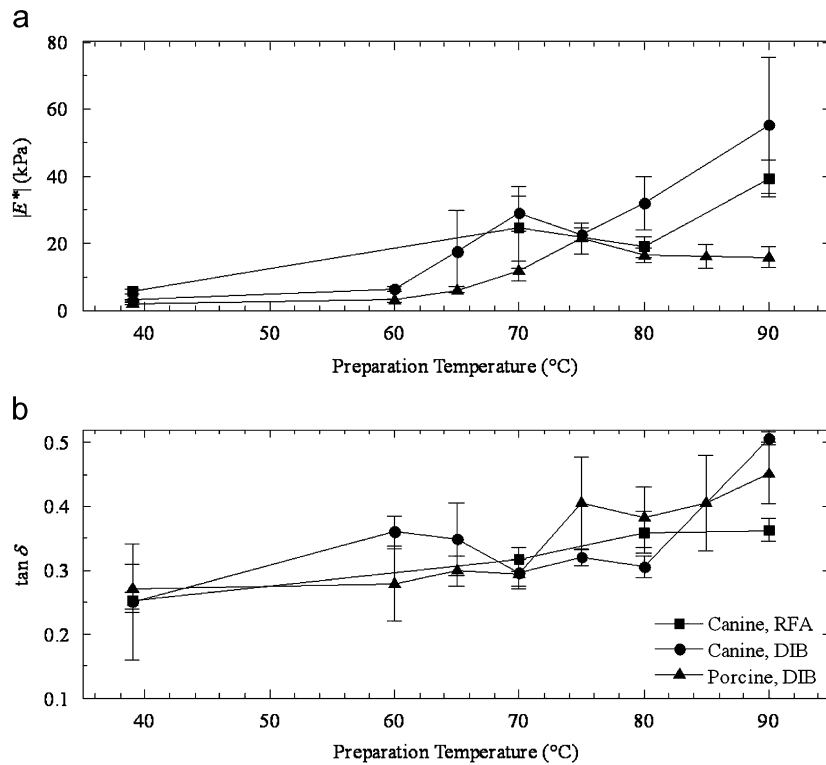


Fig. 6. Comparison of (a) the magnitude of the complex modulus and (b) $\tan \delta$ as a function of preparation temperature for all three cases at 1.0 Hz.

Corresponding results for porcine tissue are presented in Fig. 5. The peak in the modulus occurs at 75 °C (Fig. 5a), ranging from 15 kPa at 0.1 Hz up to 30 kPa at 10 Hz, and there is no recovery to

higher moduli at higher temperatures. So, unlike the results for canine tissue, the moduli of lesions at higher temperatures level off at 10 kPa at 0.1 Hz, 15 kPa at 1 Hz, and there is a small upturn

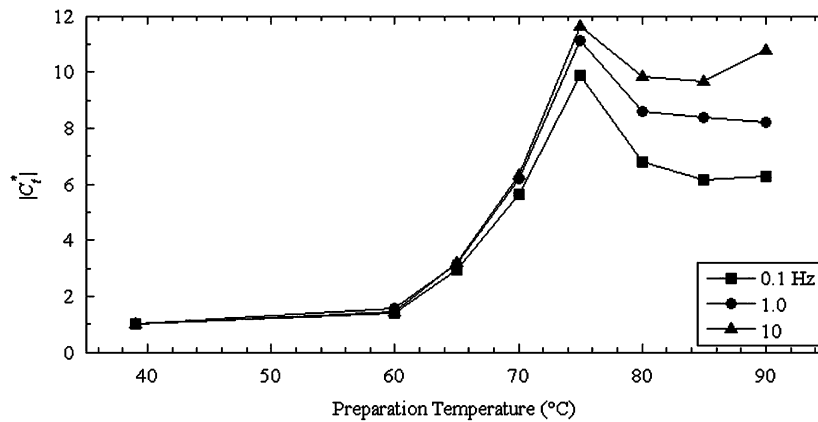


Fig. 7. Magnitude of the complex modulus contrast as a function of the preparation temperature for porcine liver prepared by DIB.

towards 30 kPa at 10 Hz. The phase information in Fig. 5b occupies a slightly larger range in values from 0.275 to 0.55 compared to Fig. 4b, and there is a rapid increase from 70 to 75 °C corresponding to the peak in Fig. 4a.

Fig. 6 is a direct comparison of the (a) magnitude and (b) phase of the complex modulus as a function of lesion temperature at 1.0 Hz for all three tissue/lesion types. In Fig. 6a, the local maximum at 70 or 75 °C is clear, and the difference in high temperature is striking, with the canine temperature results exceeding 30 kPa and the porcine tissue around 15 kPa at 90 °C. In Fig. 6b, the phase generally increases with temperature in every case, although the features around 70 or 75 °C are apparent.

Fig. 7 shows the modulus contrast as defined in Eq. (6) for porcine liver for the three frequencies as shown in Fig. 5. These values were obtained by dividing the magnitude of the lesion modulus by the normal tissue modulus. The data point below 40 °C corresponds to the normal tissue divided by itself and is equal to 1. It is included in the plot as a reference for the other values.

4. Discussion

The primary mechanism for altering the stiffness properties in soft tissues is the change in configurational entropy (Chen and Humphrey, 1998; Wu et al., 2001). Thermal ablation increases the entropy via heat-induced denaturation, where protein structures are transformed from their native helical structures into more disordered coiled structures (Privalov, 1982). As biological tissue is subjected to high temperatures (well above the normal environment), heat shock can cause a cell to lose viability and induce cell death if there are insufficient defense mechanisms in place. Cell death can occur either by apoptosis or necrosis. Apoptosis is a highly regulated process of programmed cell death that occurs from 42 to 46 °C (Badini et al., 2003), essentially cell suicide, in which the cell initially releases heat shock proteins intended to protect from thermal stress injury. In the case of exposure to sustained thermal stresses or high temperatures, excess production of these proteins eventually leads to cell death (Badini et al., 2003; Samali et al., 1999). Necrosis occurs when the damage to a cell is so severe that it cannot repair itself or provide adequate defensive measures. This damage can occur due to temperatures much higher than 46 °C, so that the apoptotic program does not execute. The contents of the damaged cell are released into the surrounding environment.

Although the experiments conducted here were conducted *ex vivo*, that is, on excised tissue specimens, the cause of cell death is

less important than the mechanisms leading to the stiffness changes at various temperatures. The local maximum in the magnitude of the modulus near 70 °C is apparent in Figs. 3–6. Bharat et al. (2005) have reported this feature in temperature-dependent results in direct context to modulus and strain contrast in elastography. The plots in Fig. 7 also show variation for a tissue specimen tested in the paper. The general shape is similar to that of Fig. 5, with the tissue prepared at 75 °C being almost 12 times as stiff as normal tissue at 10 Hz. However, a search through the literature suggests that this feature in liver tissue may not have been observed or reported on before now, although other temperature-dependent properties, such as the ultrasonic properties (Gertner et al., 1997; Techavipoo et al., 2002), dielectric properties (Chin and Sherar, 2001), and the extent of protein denaturation of hepatocytes during heat shock (Lepock et al., 1993) have been reported. An inspection of the food science literature reveals that this particular feature is hinted at in skeletal muscle (i.e., meat is hinted by McGee (1984)).

It is known that protein molecules begin to uncoil (undergo denaturation) at roughly 38 °C, and begin to shorten at temperatures as low as 54 °C. As the tissue coagulates, water in the cells is forced out. At 77 °C, the cells have shrunk as much as they can and most of the water in the cells that can be released through tissue coagulation has occurred (McGee, 1984; Wiederhorn and Reardon, 1952). The contraction of tissue and fluid loss manifests itself as increase in the complex modulus. Thus, the peak noted in the figures is believed to represent the point where liver tissue has shrunk to its minimal size. For temperatures above this threshold, the decrease in the modulus is likely due to the fact that the collagen content is being converted to gelatin.

5. Conclusions

The viscoelastic properties of thermal lesions created in *ex vivo* animal tissue have been measured as functions of both the mechanical testing frequency as well as the lesion preparation temperature. The frequency-dependence generally followed the behavior documented in the literature (Kiss et al., 2004), but the temperature-dependence showed a local maximum in the modulus that had not been reported before. The local maximum suggests that there may be a tradeoff in the optimal treatment temperature and the optimal strain contrast temperature. Results like these should allow investigators in elastography to predict the level of strain contrast in an elastogram of thermal lesions, given a particular temperature. This could lead to further development of elastography as a diagnostic tool used during minimally invasive

surgical procedures such as RF ablation of hepatic tumors or other pathologies of the liver.

Further work is required in this area, including computer simulations and experiments at the cellular level in order to further understand the relationship between the viscoelastic properties and the strain contrast. Additionally, mechanical testing relying on shear motion instead of compression will also be considered. As the understanding of the mechanical properties improves, other tissue types will be investigated including human tissue, which would provide the most realistic results.

Conflict of interest

None

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